



School, neighbourhood and family contributions to pupils' progress

Jon Rasbash, George Leckie, Rebecca Pillinger and Jenny Jenkins

1. Partitioning variation in progress

What do we already know?

| Response Predictors | ① | | ② | ③ | ④ | | ⑤ | | ⑥ | ⑦ | | ⑧ |
|---------------------|--------|--------|--------|--------|-------|--------|-------|--------|-------|---------|--------|-------|
| | Prog Y | Prog Y | Prog Y | Att N | Att N | Prog Y | Att N | Prog Y | Att N | Att N | Prog Y | Cog N |
| LEA Neighbhd | | | 0.2 | 3 2 | 20 | 4 | 14 | 1 | 5 | 4 | 1 | 0.20 |
| Secondary Primary | 5–20 | 5–20 | 5 | 22 | fixed | | 7 | 1 | 20 | 23 3 | 4 7 | |
| Cohort | | | 3 | | | | | | | | | 0.21 |
| Pupil | 80–95 | 80–95 | 93 | 73 | 80 | 96 | 79 | 98 | 75 | 70 | 88 | |
| MZ twins | | | | | | | | | | | | 0.78 |
| DZ twins | | | | | | | | | | | | 0.64 |
| Full sibs | | | | | | | | | | | | 0.51 |

- ① Typical school effectiveness studies, e.g. Goldstein et al. (2007) (primary schools) and Leckie (2008) (secondary schools)
- ② Yang & Woodhouse (2001), progress from GCSE to A-level
- ③ Fielding et al. (2006)
- ④ Garner & Raudenbush (1991); predictors include family background, neighbourhood social deprivation and school fixed effects
- ⑤ Raudenbush (1993); reanalysis of Garner & Raudenbush (1991)
- ⑥ Leckie (2009)
- ⑦ Leckie (2009)
- ⑧ Duncan et al. (2001); US data; response is Peabody Picture Vocabulary Test

What do we already know?

| Response Predictors | ① | | ② | ③ | ④ | | ⑤ | | ⑥ | ⑦ | | ⑧ |
|---------------------|--------|--------|--------|-------|-------|--------|-------|--------|-------|-------|--------|-------|
| | Prog Y | Prog Y | Prog Y | Att N | Att N | Prog Y | Att N | Prog Y | Att N | Att N | Prog Y | Cog N |
| LEA | | | 0.2 | 3 | | | | | | | | |
| Neighbhd | | | | 2 | 20 | 4 | 14 | 1 | 5 | 4 | 1 | 0.20 |
| Secondary | 5-20 | | 5 | 22 | fixed | | 7 | 1 | 20 | 23 | 4 | |
| Primary | 5-20 | | | | | | | | | 3 | 7 | |
| Cohort | | | 3 | | | | | | | | | |
| Pupil | 80-95 | 80-95 | 93 | 73 | 80 | 96 | 79 | 98 | 75 | 70 | 88 | |
| MZ twins | | | | | | | | | | | | |
| DZ twins | | | | | | | | | | | | |
| Full sibs | | | | | | | | | | | | |

- ① Typical school effectiveness studies, e.g. Goldstein et al. (2007) (primary schools) and Leckie (2008) (secondary schools)
- ② Yang & Woodhouse (2001), progress from GCSE to A-level
- ③ Fielding et al. (2006)
- ④ Garner & Raudenbush (1991); predictors include family background, neighbourhood social deprivation and school fixed effects
- ⑤ Raudenbush (1993); reanalysis of Garner & Raudenbush (1991)
- ⑥ Leckie (2009)
- ⑦ Leckie (2009)
- ⑧ Duncan et al. (2001); US data; response is Peabody Picture Vocabulary Test

What do we already know?

| Response Predictors | ① | | ② | ③ | ④ | | ⑤ | | ⑥ | ⑦ | | ⑧ |
|---------------------|--------|--------|--------|-------|-------|--------|-------|--------|-------|-------|--------|-------|
| | Prog Y | Prog Y | Prog Y | Att N | Att N | Prog Y | Att N | Prog Y | Att N | Att N | Prog Y | Cog N |
| LEA Neighbhd | | | 0.2 | 3 | 20 | 4 | 14 | 1 | 5 | 4 | 1 | 0.20 |
| Secondary Primary | 5–20 | 5–20 | 5 | 22 | fixed | | 7 | 1 | 20 | 23 | 4 | |
| Cohort | | | 3 | | | | | | | | | 0.21 |
| Pupil | 80–95 | 80–95 | 93 | 73 | 80 | 96 | 79 | 98 | 75 | 70 | 88 | |
| MZ twins | | | | | | | | | | | | 0.78 |
| DZ twins | | | | | | | | | | | | 0.64 |
| Full sibs | | | | | | | | | | | | 0.51 |

- ① Typical school effectiveness studies, e.g. Goldstein et al. (2007) (primary schools) and Leckie (2008) (secondary schools)
- ② Yang & Woodhouse (2001), progress from GCSE to A-level
- ③ Fielding et al. (2006)
- ④ Garner & Raudenbush (1991); predictors include family background, neighbourhood social deprivation and school fixed effects
- ⑤ Raudenbush (1993); reanalysis of Garner & Raudenbush (1991)
- ⑥ Leckie (2009)
- ⑦ Leckie (2009)
- ⑧ Duncan et al. (2001); US data; response is Peabody Picture Vocabulary Test

What do we already know?

| Response Predictors | ① | | ② | ③ | ④ | | ⑤ | | ⑥ | ⑦ | | ⑧ |
|---------------------|--------|--------|--------|-------|-------|--------|-------|--------|-------|-------|--------|-------|
| | Prog Y | Prog Y | Prog Y | Att N | Att N | Prog Y | Att N | Prog Y | Att N | Att N | Prog Y | Cog N |
| LEA | | | 0.2 | 3 | | | | | | | | |
| Neighbhd | | | | 2 | 20 | 4 | 14 | 1 | 5 | 4 | 1 | 0.20 |
| Secondary | 5–20 | | 5 | 22 | | fixed | 7 | 1 | 20 | 23 | 4 | |
| Primary | | 5–20 | | | | | | | | 3 | 7 | |
| Cohort | | | 3 | | | | | | | | | 0.21 |
| Pupil | 80–95 | 80–95 | 93 | 73 | 80 | 96 | 79 | 98 | 75 | 70 | 88 | |
| MZ twins | | | | | | | | | | | | 0.78 |
| DZ twins | | | | | | | | | | | | 0.64 |
| Full sibs | | | | | | | | | | | | 0.51 |

- ① Typical school effectiveness studies, e.g. Goldstein et al. (2007) (primary schools) and Leckie (2008) (secondary schools)
- ② Yang & Woodhouse (2001), progress from GCSE to A-level
- ③ Fielding et al. (2006)
- ④ Garner & Raudenbush (1991); predictors include family background, neighbourhood social deprivation and school fixed effects
- ⑤ Raudenbush (1993); reanalysis of Garner & Raudenbush (1991)
- ⑥ Leckie (2009)
- ⑦ Leckie (2009)
- ⑧ Duncan et al. (2001); US data; response is Peabody Picture Vocabulary Test

What do we already know?

| Response Predictors | ① | | ② | ③ | ④ | | ⑤ | | ⑥ | ⑦ | | ⑧ |
|---------------------|--------|--------|--------|-------|-------|--------|-------|--------|-------|-------|--------|-------|
| | Prog Y | Prog Y | Prog Y | Att N | Att N | Prog Y | Att N | Prog Y | Att N | Att N | Prog Y | Cog N |
| LEA | | | 0.2 | 3 | | | | | | | | |
| Neighbhd | | | | 2 | 20 | 4 | 14 | 1 | 5 | 4 | 1 | 0.20 |
| Secondary | 5–20 | | 5 | 22 | fixed | | 7 | 1 | 20 | 23 | 4 | |
| Primary | | 5–20 | | | | | | | | 3 | 7 | |
| Cohort | | | 3 | | | | | | | | | 0.21 |
| Pupil | 80–95 | 80–95 | 93 | 73 | 80 | 96 | 79 | 98 | 75 | 70 | 88 | |
| MZ twins | | | | | | | | | | | | 0.78 |
| DZ twins | | | | | | | | | | | | 0.64 |
| Full sibs | | | | | | | | | | | | 0.51 |

- ① Typical school effectiveness studies, e.g. Goldstein et al. (2007) (primary schools) and Leckie (2008) (secondary schools)
- ② Yang & Woodhouse (2001), progress from GCSE to A-level
- ③ Fielding et al. (2006)
- ④ Garner & Raudenbush (1991); predictors include family background, neighbourhood social deprivation and school fixed effects
- ⑤ Raudenbush (1993); reanalysis of Garner & Raudenbush (1991)
- ⑥ Leckie (2009)
- ⑦ Leckie (2009)
- ⑧ Duncan et al. (2001); US data; response is Peabody Picture Vocabulary Test

What do we already know?

| Response Predictors | ① | | ② | ③ | ④ | | ⑤ | | ⑥ | ⑦ | | ⑧ |
|---------------------|--------|--------|--------|-------|-------|--------|-------|--------|-------|-------|--------|-------|
| | Prog Y | Prog Y | Prog Y | Att N | Att N | Prog Y | Att N | Prog Y | Att N | Att N | Prog Y | Cog N |
| LEA | | | 0.2 | 3 | | | | | | | | |
| Neighbhd | | | | 2 | 20 | 4 | 14 | 1 | 5 | 4 | 1 | 0.20 |
| Secondary | 5–20 | | 5 | 22 | | fixed | 7 | 1 | 20 | 23 | 4 | |
| Primary | | 5–20 | | | | | | | | 3 | 7 | |
| Cohort | | | 3 | | | | | | | | | 0.21 |
| Pupil | 80–95 | 80–95 | 93 | 73 | 80 | 96 | 79 | 98 | 75 | 70 | 88 | |
| MZ twins | | | | | | | | | | | | 0.78 |
| DZ twins | | | | | | | | | | | | 0.64 |
| Full sibs | | | | | | | | | | | | 0.51 |

- ① Typical school effectiveness studies, e.g. Goldstein et al. (2007) (primary schools) and Leckie (2008) (secondary schools)
- ② Yang & Woodhouse (2001), progress from GCSE to A-level
- ③ Fielding et al. (2006)
- ④ Garner & Raudenbush (1991); predictors include family background, neighbourhood social deprivation and school fixed effects
- ⑤ Raudenbush (1993); reanalysis of Garner & Raudenbush (1991)
- ⑥ Leckie (2009)
- ⑦ Leckie (2009)
- ⑧ Duncan et al. (2001); US data; response is Peabody Picture Vocabulary Test

What do we already know?

| Response Predictors | ① | | ② | ③ | ④ | | ⑤ | | ⑥ | ⑦ | | ⑧ |
|---------------------|--------|--------|--------|-------|-------|--------|-------|--------|-------|-------|--------|-------|
| | Prog Y | Prog Y | Prog Y | Att N | Att N | Prog Y | Att N | Prog Y | Att N | Att N | Prog Y | Cog N |
| LEA | | | 0.2 | 3 | | | | | | | | |
| Neighbhd | | | | 2 | 20 | 4 | 14 | 1 | 5 | 4 | 1 | 0.20 |
| Secondary | 5–20 | | 5 | 22 | fixed | | 7 | 1 | 20 | 23 | 4 | |
| Primary | | 5–20 | | | | | | | | 3 | 7 | |
| Cohort | | | 3 | | | | | | | | | 0.21 |
| Pupil | 80–95 | 80–95 | 93 | 73 | 80 | 96 | 79 | 98 | 75 | 70 | 88 | |
| MZ twins | | | | | | | | | | | | 0.78 |
| DZ twins | | | | | | | | | | | | 0.64 |
| Full sibs | | | | | | | | | | | | 0.51 |

- ① Typical school effectiveness studies, e.g. Goldstein et al. (2007) (primary schools) and Leckie (2008) (secondary schools)
- ② Yang & Woodhouse (2001), progress from GCSE to A-level
- ③ Fielding et al. (2006)
- ④ Garner & Raudenbush (1991); predictors include family background, neighbourhood social deprivation and school fixed effects
- ⑤ Raudenbush (1993); reanalysis of Garner & Raudenbush (1991)
- ⑥ Leckie (2009)
- ⑦ Leckie (2009)
- ⑧ Duncan et al. (2001); US data; response is Peabody Picture Vocabulary Test

What do we already know?

| Response Predictors | ① | ② | ③ | ④ | ⑤ | ⑥ | ⑦ | ⑧ | ⑨ | ⑩ | ⑪ | ⑫ |
|------------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| | Att N | Att N | Att N | Att N | Att N | Att N | Att N | Att N | Att N | Att N | Att N | Att N |
| LEA | | | | | | | | | | | | |
| Neighbhd | | | | | | | | | | | | |
| Secondary | | | | | | | | | | | | |
| Primary | | | | | | | | | | | | |
| Cohort | | | | | | | | | | | | |
| Non-shared envt | 0 | 43 | 10 | 10 | 6 | 11 | 24 | 29 | 14 | 9 | 23 | 24 |
| Genetic | 38 | 21 | 17 | 53 | 28 | 53 | 60 | 36 | 67 | 67 | 68 | 49 |
| Shared envt | 62 | 36 | 73 | 37 | 66 | 36 | 16 | 35 | 19 | 24 | 9 | 27 |

- ① Cardon et al. (1990); reading recognition
- ② Brooks et al. (1990); spelling
- ③ Thompson et al. (1991); maths
- ④ Thompson et al. (1993); composite of WRAT-R and MAT
- ⑤ Petrill & Thompson (1993); MAT
- ⑥ Petrill & Thompson (1994); MAT
- ⑦ Van den Oord & Rowe (1997); PIAT
- ⑧ Cleveland et al. (2000); composite of PPVT and PIATS
- ⑨ Wainwright et al. (2005); QCST, Australian data
- ⑩ Friend et al. (2007); spelling production (WRAT)
- ⑪ Haworth et al. (2007); maths, UK data
- ⑫ Haworth et al. (2008); science, UK data

Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)

Developmental Psychology

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school

Developmental Psychology

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family

Developmental Psychology

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family
- The largest component of variation in these models is the pupil level

Developmental Psychology

Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Developmental Psychology

Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Developmental Psychology

- ▣ Models usually have children within families

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family
- The largest component of variation in these models is the pupil level
- How much of that is really family level?

Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family
- The largest component of variation in these models is the pupil level
- How much of that is really family level?

Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment
- What is the shared environment?

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family
- The largest component of variation in these models is the pupil level
- How much of that is really family level?

Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment
- What is the shared environment?
- In other words, How much of the shared environment is family, school and area?

Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Classification diagram



Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Classification diagram



Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Classification diagram

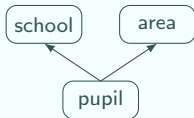


Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Classification diagram

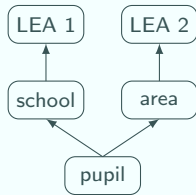


Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Classification diagram

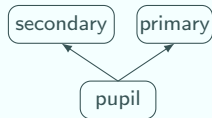


Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Classification diagram

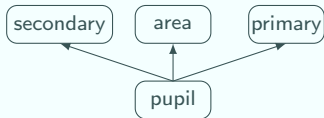


Previous studies

School effectiveness

- ▣ Models usually have pupils within schools (2 levels)
- ▣ There have been studies that also included area or primary school
- ▣ But no studies have included family
- ▣ The largest component of variation in these models is the pupil level
- ▣ How much of that is really family level?

Classification diagram



Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family
- The largest component of variation in these models is the pupil level
- How much of that is really family level?

Classification diagram



Model

$$y_{ij} = \alpha + \beta x_{ij} + u_j + e_{ij},$$

$$u_j \sim N(0, \sigma_u^2), \quad i = 1, \dots, n_j$$
$$e_{ij} \sim N(0, \sigma_e^2), \quad j = 1, \dots, J$$

(B)

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family
- The largest component of variation in these models is the pupil level
- How much of that is really family level?

Classification diagram



Model

$$\text{GCSE}_{ij} = \alpha + \beta \text{pretest}_{ij} + u_j + e_{ij},$$

$$u_j \sim N(0, \sigma_u^2), \quad i = 1, \dots, n_j$$
$$e_{ij} \sim N(0, \sigma_e^2), \quad j = 1, \dots, J$$

(B)

Previous studies

School effectiveness

- Models usually have pupils within schools (2 levels)
- There have been studies that also included area or primary school
- But no studies have included family
- The largest component of variation in these models is the pupil level
- How much of that is really family level?

Classification diagram



Model

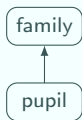
$$\text{GCSE}_{ij} = \alpha + \beta_1 \text{pretest}_{ij} + \beta_2 x_{ij} + u_j + e_{ij},$$

$$u_j \sim N(0, \sigma_u^2), \quad i = 1, \dots, n_j$$
$$e_{ij} \sim N(0, \sigma_e^2), \quad j = 1, \dots, J$$

(B)

Previous studies

Classification diagram

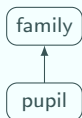


Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment
- What is the shared environment?
- In other words, **How much of the shared environment is family, school and area?**

Previous studies

Classification diagram



Model

$$y_{ij} = \alpha + u_j + e_{ij} + g_{ij}$$

$$u_j \sim N(0, \sigma_u^2)$$

$$e_{ij} \sim N(0, \sigma_e^2)$$

$$g_{ij} \sim N(0, \sigma_g^2)$$

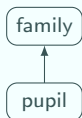
$$\text{Cov}(g_{i_1j}, g_{i_2j}) = r_{(i_1j, i_2j)} \sigma_g^2$$

Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment
- What is the shared environment?
- In other words, **How much of the shared environment is family, school and area?**

Previous studies

Classification diagram



Model

$$y_{ij} = \alpha + d_j u_{1j} + d_j e_{1ij} + (1 - d_j) e_{2ij}$$

$$u_{1j} \sim N(0, \sigma_u^2)$$

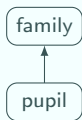
$$\begin{bmatrix} e_{1ij} \\ e_{2ij} \end{bmatrix} \sim N \left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \sigma_{e1}^2 & \\ 0 & \sigma_{e2}^2 \end{bmatrix} \right)$$

Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment
- What is the shared environment?
- In other words, **How much of the shared environment is family, school and area?**

Previous studies

Classification diagram



Model

$$\text{GCSE}_{ij} = \alpha + u_{1j}\text{twin}_j + e_{1ij}\text{twin}_j \\ + e_{2ij}\text{nontwin}_j$$

$$u_{1j} \sim N(0, \sigma_u^2)$$

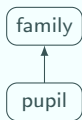
$$\begin{bmatrix} e_{1ij} \\ e_{2ij} \end{bmatrix} \sim N \left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \sigma_{e1}^2 & 0 \\ 0 & \sigma_{e2}^2 \end{bmatrix} \right)$$

Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment
- What is the shared environment?
- In other words, **How much of the shared environment is family, school and area?**

Previous studies

Classification diagram



Model

$$\begin{aligned} \text{GCSE}_{ij} = & \alpha + \beta_1 \text{pretest}_{ij} + \beta_2 \text{twin} \\ & + \beta_3 \text{twin}_j \cdot \text{pretest}_{ij} \\ & + u_{1j} \text{twin}_j + e_{1ij} \text{twin}_j \\ & + e_{2ij} \text{nontwin}_j \end{aligned}$$

$$u_{1j} \sim N(0, \sigma_u^2),$$

$$\begin{bmatrix} e_{1ij} \\ e_{2ij} \end{bmatrix} \sim N \left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \sigma_{e1}^2 & \\ 0 & \sigma_{e2}^2 \end{bmatrix} \right)$$

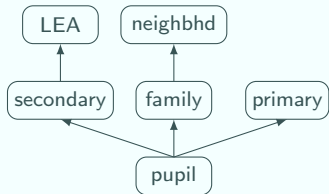
(A)

Developmental Psychology

- Models usually have children within families
- Researchers recognise that really these models partition into shared environment and non-shared environment
- What is the shared environment?
- In other words, **How much of the shared environment is family, school and area?**

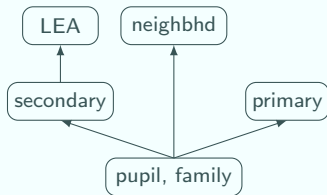
Our model

Classification diagram



Our model

Classification diagram



Our model

Model

$$y_i = \alpha + \beta x_i + u_{LEA(i)}^{(6)} + u_{sec(i)}^{(5)} + u_{nbhd(i)}^{(4)} + u_{pri(i)}^{(3)} \\ + u_{fam(i)}^{(2)} d_{fam(i)} + e_{1i} d_{fam(i)} + e_{2i} (1 - d_{fam(i)})$$

$$u_{LEA(i)}^{(6)} \sim N(0, \sigma_{u^{(6)}}^2)$$

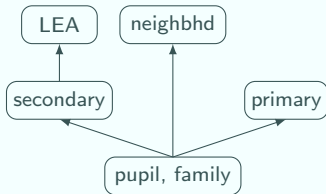
\vdots $\quad \quad \quad \vdots$

$$u_{pri(i)}^{(3)} \sim N(0, \sigma_{u^{(3)}}^2)$$

$$u_{fam(i)}^{(2)} \sim N(0, \sigma_{u^{(2)}}^2)$$

$$\begin{bmatrix} e_{1i} \\ e_{2i} \end{bmatrix} \sim N\left(0, \begin{bmatrix} \sigma_{e1}^2 & \\ 0 & \sigma_{e2}^2 \end{bmatrix}\right) \quad (C)$$

Classification diagram



Our model

Model

$$\begin{aligned} \text{GCSE}_i = & \alpha + \beta_1 \text{pretest}_i + \beta_2 \text{twin}_i + \beta_3 \text{pretest} \cdot \text{twin}_i \\ & + u_{\text{LEA}(i)}^{(6)} + u_{\text{sec}(i)}^{(5)} + u_{\text{nbhd}(i)}^{(4)} + u_{\text{pri}(i)}^{(3)} \\ & + u_{\text{fam}(i)}^{(2)} \text{twin}_{\text{fam}(i)} + e_{1i} \text{twin}_{\text{fam}(i)} + e_{2i} \text{nontwin}_{\text{fam}(i)} \end{aligned}$$

$$u_{\text{LEA}(i)}^{(6)} \sim N(0, \sigma_{u^{(6)}}^2)$$

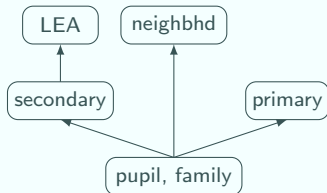
\vdots

$$u_{\text{pri}(i)}^{(3)} \sim N(0, \sigma_{u^{(3)}}^2)$$

$$u_{\text{fam}(i)}^{(2)} \sim N(0, \sigma_{u^{(2)}}^2)$$

$$\begin{bmatrix} e_{1i} \\ e_{2i} \end{bmatrix} \sim N\left(0, \begin{bmatrix} \sigma_{e1}^2 & \\ 0 & \sigma_{e2}^2 \end{bmatrix}\right) \quad (C)$$

Classification diagram



Our data

Sample

All pupils in

- England
- state schools
- 2007 GCSE cohort

Our data

Sample

All pupils in

- England
- state schools
- 2007 GCSE cohort

Variables

- Test scores from the NPD
 - GCSE (our response) and
 - key stage 2 (KS2)

All continuous variables have been standardized

Our data

Sample

All pupils in

- England
- state schools
- 2007 GCSE cohort

Variables

- Test scores from the NPD
 - GCSE (our response) and
 - key stage 2 (KS2)
- Background characteristics from PLASC
 - age
 - gender
 - ethnicity
 - FSM eligibility
 - SEN
 - EAL

All continuous variables have been standardized

Our data

Sample

All pupils in

- England
- state schools
- 2007 GCSE cohort

Variables

- Test scores from the NPD
 - GCSE (our response) and
 - key stage 2 (KS2)
- Background characteristics from PLASC
 - age
 - gender
 - ethnicity
 - FSM eligibility
 - SEN
 - EAL
- ONS data on LSOAs
 - IDACI

All continuous variables have been standardized

Our data

Sample

All pupils in

- England
- state schools
- 2007 GCSE cohort

Levels

- The data records which
 - LEA
 - secondary school
 - primary school
 - area (LSOA)
- each pupil belongs to

Variables

- Test scores from the NPD
 - GCSE (our response) and
 - key stage 2 (KS2)
- Background characteristics from PLASC
 - age
 - gender
 - ethnicity
 - FSM eligibility
 - SEN
 - EAL
- ONS data on LSOAs
 - IDACI

All continuous variables have been standardized

Our data

Sample

All pupils in

- ▣ England
- ▣ state schools
- ▣ 2007 GCSE cohort

Levels

- ▣ The data records which
 - ▣ LEA
 - ▣ secondary school
 - ▣ primary school
 - ▣ area (LSOA)each pupil belongs to
- ▣ But not which family

Variables

- ▣ Test scores from the NPD
 - ▣ GCSE (our response) and
 - ▣ key stage 2 (KS2)
- ▣ Background characteristics from PLASC
 - ▣ age
 - ▣ gender
 - ▣ ethnicity
 - ▣ FSM eligibility
 - ▣ SEN
 - ▣ EAL
- ▣ ONS data on LSOAs
 - ▣ IDACI

All continuous variables have been standardized

Our data

Identifying twins

- We get the family level by identifying twin pairs

Our data

Identifying twins

- We get the family level by identifying twin pairs
- by matching on time invariant characteristics
 - date of birth
 - ethnicity
 - EAL

Our data

Identifying twins

- We get the family level by identifying twin pairs
- by matching on time invariant characteristics

- date of birth
- ethnicity
- EAL

and pattern of time-varying characteristics

- postcode sector
- FSM eligibility

Our data

Identifying twins

- We get the family level by identifying twin pairs
- by matching on time invariant characteristics

- date of birth
- ethnicity
- EAL

and pattern of time-varying characteristics

- postcode sector
- FSM eligibility

How successful is this?

- 11.54 twin births per 1000 maternities in 1990 & 1991

Our data

Identifying twins

- We get the family level by identifying twin pairs
- by matching on time invariant characteristics

- date of birth
- ethnicity
- EAL

and pattern of time-varying characteristics

- postcode sector
- FSM eligibility

How successful is this?

- 11.54 twin births per 1000 maternities in 1990 & 1991
- 9.37 twin pairs per 1000 families in our matching

Our data

Identifying twins

- We get the family level by identifying twin pairs
- by matching on time invariant characteristics

- date of birth
- ethnicity
- EAL

and pattern of time-varying characteristics

- postcode sector
- FSM eligibility

How successful is this?

- 11.54 twin births per 1000 maternities in 1990 & 1991
- 9.37 twin pairs per 1000 families in our matching
- We may also have labelled some unrelated pupils as a 'twin pair'

Our data

Identifying twins

- We get the family level by identifying twin pairs
- by matching on time invariant characteristics

- date of birth
- ethnicity
- EAL

and pattern of time-varying characteristics

- postcode sector
- FSM eligibility

How successful is this?

- 11.54 twin births per 1000 maternities in 1990 & 1991
- 9.37 twin pairs per 1000 families in our matching
- We may also have labelled some unrelated pupils as a 'twin pair'
- Calculation suggests around 10% of 'twin pairs' will be coincidental matches

Our data

Identifying twins

- We get the family level by identifying twin pairs
- by matching on time invariant characteristics

- date of birth
- ethnicity
- EAL

and pattern of time-varying characteristics

- postcode sector
- FSM eligibility

How successful is this?

- 11.54 twin births per 1000 maternities in 1990 & 1991
- 9.37 twin pairs per 1000 families in our matching
- We may also have labelled some unrelated pupils as a 'twin pair'
- Calculation suggests around 10% of 'twin pairs' will be coincidental matches

Size of dataset

551,220 pupils

5116 twin pairs

30507 LSOAs

14765 primaries

3099 secondaries

149 LEAs

Results

| | Model A | | Model B | | Model C | | Model D | |
|------------------|---------|---------|---------|---------|---------|---------|---------|---------|
| cons | -0.003 | (0.001) | -0.003 | (0.001) | 0.001 | (0.008) | -0.039 | (0.007) |
| twin | 0.177 | (0.008) | 0.179 | (0.007) | 0.162 | (0.007) | 0.154 | (0.007) |
| pretest | 0.730 | (0.001) | 0.729 | (0.001) | 0.701 | (0.001) | 0.641 | (0.001) |
| pretest.twin | -0.040 | (0.007) | 0.000 | (0.007) | -0.027 | (0.006) | -0.020 | (0.006) |
| female | | | | | | | 0.184 | (0.002) |
| Asian | | | | | | | 0.429 | (0.005) |
| Black | | | | | | | 0.225 | (0.006) |
| Chinese | | | | | | | 0.556 | (0.015) |
| Mixed | | | | | | | 0.045 | (0.005) |
| Other | | | | | | | 0.403 | (0.010) |
| FSM | | | | | | | -0.248 | (0.003) |
| age | | | | | | | -0.012 | (0.000) |
| SEN | | | | | | | -0.231 | (0.003) |
| IDACI | | | | | | | -0.103 | (0.001) |
| LEA | | | | | 0.005 | (0.001) | 0.005 | (0.001) |
| Secondary | | | 0.065 | (0.002) | 0.043 | (0.001) | 0.035 | (0.001) |
| Primary | | | | | 0.035 | (0.001) | 0.025 | (0.000) |
| LSOA | | | | | 0.008 | (0.000) | 0.002 | (0.000) |
| Family (twin) | 0.238 | (0.007) | | | 0.168 | (0.005) | 0.157 | (0.005) |
| Pupil (twin) | 0.160 | (0.003) | | | 0.157 | (0.003) | 0.150 | (0.003) |
| Pupil (non-twin) | 0.468 | (0.001) | 0.402 | (0.002) | 0.383 | (0.001) | 0.357 | (0.001) |

Using MCMC; 450,500 iterations and a burn-in of 50,000

Results

| | Model A | | Model B | | Model C | | Model D | |
|------------------|---------|---------|---------|---------|---------|---------|---------|---------|
| cons | -0.003 | (0.001) | -0.003 | (0.001) | 0.001 | (0.008) | -0.039 | (0.007) |
| twin | 0.177 | (0.008) | 0.179 | (0.007) | 0.162 | (0.007) | 0.154 | (0.007) |
| pretest | 0.730 | (0.001) | 0.729 | (0.001) | 0.701 | (0.001) | 0.641 | (0.001) |
| pretest.twin | -0.040 | (0.007) | 0.000 | (0.007) | -0.027 | (0.006) | -0.020 | (0.006) |
| female | | | | | | | 0.184 | (0.002) |
| Asian | | | | | | | 0.429 | (0.005) |
| Black | | | | | | | 0.225 | (0.006) |
| Chinese | | | | | | | 0.556 | (0.015) |
| Mixed | | | | | | | 0.045 | (0.005) |
| Other | | | | | | | 0.403 | (0.010) |
| FSM | | | | | | | -0.248 | (0.003) |
| age | | | | | | | -0.012 | (0.000) |
| SEN | | | | | | | -0.231 | (0.003) |
| IDACI | | | | | | | -0.103 | (0.001) |
| LEA | | | | | 0.005 | (0.001) | 0.005 | (0.001) |
| Secondary | | | 0.065 | (0.002) | 0.043 | (0.001) | 0.035 | (0.001) |
| Primary | | | | | 0.035 | (0.001) | 0.025 | (0.000) |
| LSOA | | | | | 0.008 | (0.000) | 0.002 | (0.000) |
| Family (twin) | 0.238 | (0.007) | | | 0.168 | (0.005) | 0.157 | (0.005) |
| Pupil (twin) | 0.160 | (0.003) | | | 0.157 | (0.003) | 0.150 | (0.003) |
| Pupil (non-twin) | 0.468 | (0.001) | 0.402 | (0.002) | 0.383 | (0.001) | 0.357 | (0.001) |

Using MCMC; 450,500 iterations and a burn-in of 50,000

Results

| | Model A | | Model B | | Model C | | Model D | |
|------------------|---------|---------|---------|---------|---------|---------|---------|---------|
| cons | -0.003 | (0.001) | -0.003 | (0.001) | 0.001 | (0.008) | -0.039 | (0.007) |
| twin | 0.177 | (0.008) | 0.179 | (0.007) | 0.162 | (0.007) | 0.154 | (0.007) |
| pretest | 0.730 | (0.001) | 0.729 | (0.001) | 0.701 | (0.001) | 0.641 | (0.001) |
| pretest.twin | -0.040 | (0.007) | 0.000 | (0.007) | -0.027 | (0.006) | -0.020 | (0.006) |
| female | | | | | | | 0.184 | (0.002) |
| Asian | | | | | | | 0.429 | (0.005) |
| Black | | | | | | | 0.225 | (0.006) |
| Chinese | | | | | | | 0.556 | (0.015) |
| Mixed | | | | | | | 0.045 | (0.005) |
| Other | | | | | | | 0.403 | (0.010) |
| FSM | | | | | | | -0.248 | (0.003) |
| age | | | | | | | -0.012 | (0.000) |
| SEN | | | | | | | -0.231 | (0.003) |
| IDACI | | | | | | | -0.103 | (0.001) |
| LEA | | | | | 0.005 | (0.001) | 0.005 | (0.001) |
| Secondary | | | 0.065 | (0.002) | 0.043 | (0.001) | 0.035 | (0.001) |
| Primary | | | | | 0.035 | (0.001) | 0.025 | (0.000) |
| LSOA | | | | | 0.008 | (0.000) | 0.002 | (0.000) |
| Family (twin) | 0.238 | (0.007) | | | 0.168 | (0.005) | 0.157 | (0.005) |
| Pupil (twin) | 0.160 | (0.003) | | | 0.157 | (0.003) | 0.150 | (0.003) |
| Pupil (non-twin) | 0.468 | (0.001) | 0.402 | (0.002) | 0.383 | (0.001) | 0.357 | (0.001) |

Using MCMC; 450,500 iterations and a burn-in of 50,000

Results

| | Model A | | Model B | | Model C | | Model D | |
|------------------|---------|---------|---------|---------|---------|---------|---------|---------|
| cons | -0.003 | (0.001) | -0.003 | (0.001) | 0.001 | (0.008) | -0.039 | (0.007) |
| twin | 0.177 | (0.008) | 0.179 | (0.007) | 0.162 | (0.007) | 0.154 | (0.007) |
| pretest | 0.730 | (0.001) | 0.729 | (0.001) | 0.701 | (0.001) | 0.641 | (0.001) |
| pretest.twin | -0.040 | (0.007) | 0.000 | (0.007) | -0.027 | (0.006) | -0.020 | (0.006) |
| female | | | | | | | 0.184 | (0.002) |
| Asian | | | | | | | 0.429 | (0.005) |
| Black | | | | | | | 0.225 | (0.006) |
| Chinese | | | | | | | 0.556 | (0.015) |
| Mixed | | | | | | | 0.045 | (0.005) |
| Other | | | | | | | 0.403 | (0.010) |
| FSM | | | | | | | -0.248 | (0.003) |
| age | | | | | | | -0.012 | (0.000) |
| SEN | | | | | | | -0.231 | (0.003) |
| IDACI | | | | | | | -0.103 | (0.001) |
| LEA | | | | | 0.005 | (0.001) | 0.005 | (0.001) |
| Secondary | | | 0.065 | (0.002) | 0.043 | (0.001) | 0.035 | (0.001) |
| Primary | | | | | 0.035 | (0.001) | 0.025 | (0.000) |
| LSOA | | | | | 0.008 | (0.000) | 0.002 | (0.000) |
| Family (twin) | 0.238 | (0.007) | | | 0.168 | (0.005) | 0.157 | (0.005) |
| Pupil (twin) | 0.160 | (0.003) | | | 0.157 | (0.003) | 0.150 | (0.003) |
| Pupil (non-twin) | 0.468 | (0.001) | 0.402 | (0.002) | 0.383 | (0.001) | 0.357 | (0.001) |

Using MCMC; 450,500 iterations and a burn-in of 50,000

Variance partitioning coefficients

| | A | B | C | | D | |
|-----------|-------|-------|-------|-----------|-------|-----------|
| | | | Twins | Non-twins | Twins | Non-twins |
| LEA | | | 1.2% | 1.1% | 1.3% | 1.2% |
| Secondary | | 13.9% | 10.3% | 9.1% | 9.4% | 8.3% |
| Primary | | | 8.4% | 7.4% | 6.7% | 5.9% |
| LSOA | | | 1.9% | 1.7% | 0.5% | 0.5% |
| Family | 59.8% | | 40.4% | | 42.0% | |
| Pupil | 40.2% | 86.1% | 37.7% | 80.8% | 40.1% | 84.2% |

Research questions

Variance partitioning coefficients

| | A | B | C | | D | |
|-----------|-------|-------|-------|-----------|-------|-----------|
| | | | Twins | Non-twins | Twins | Non-twins |
| LEA | | | 1.2% | 1.1% | 1.3% | 1.2% |
| Secondary | | 13.9% | 10.3% | 9.1% | 9.4% | 8.3% |
| Primary | | | 8.4% | 7.4% | 6.7% | 5.9% |
| LSOA | | | 1.9% | 1.7% | 0.5% | 0.5% |
| Family | 59.8% | | 40.4% | | 42.0% | |
| Pupil | 40.2% | 86.1% | 37.7% | 80.8% | 40.1% | 84.2% |

Research questions

1. How much of the shared environmental variation is due to family, school and area?

Variance partitioning coefficients

| | A | B | C | | D | |
|-----------|-------|-------|-------|-----------|-------|-----------|
| | | | Twins | Non-twins | Twins | Non-twins |
| LEA | | | 1.2% | 1.1% | 1.3% | 1.2% |
| Secondary | | 13.9% | 10.3% | 9.1% | 9.4% | 8.3% |
| Primary | | | 8.4% | 7.4% | 6.7% | 5.9% |
| LSOA | | | 1.9% | 1.7% | 0.5% | 0.5% |
| Family | 59.8% | | 40.4% | | 42.0% | |
| Pupil | 40.2% | 86.1% | 37.7% | 80.8% | 40.1% | 84.2% |

Research questions

1. How much of the shared environmental variation is due to family, school and area?
2. How much of the 'pupil' level variation in school effectiveness studies is really family level?

Variance partitioning coefficients

| | A | B | C | | D | |
|-----------|-------|-------|-------|-----------|-------|-----------|
| | | | Twins | Non-twins | Twins | Non-twins |
| LEA | | | 1.2% | 1.1% | 1.3% | 1.2% |
| Secondary | | 13.9% | 10.3% | 9.1% | 9.4% | 8.3% |
| Primary | | | 8.4% | 7.4% | 6.7% | 5.9% |
| LSOA | | | 1.9% | 1.7% | 0.5% | 0.5% |
| Family | 59.8% | | 40.4% | | 42.0% | |
| Pupil | 40.2% | 86.1% | 37.7% | 80.8% | 40.1% | 84.2% |

Research questions

1. How much of the shared environmental variation is due to family, school and area?
2. How much of the 'pupil' level variation in school effectiveness studies is really family level?

Variance partitioning coefficients

| | A | B | C | | D | |
|-----------|-------|-------|-------|-----------|-------|-----------|
| | | | Twins | Non-twins | Twins | Non-twins |
| LEA | | | 1.2% | 1.1% | 1.3% | 1.2% |
| Secondary | | 13.9% | 10.3% | 9.1% | 9.4% | 8.3% |
| Primary | | | 8.4% | 7.4% | 6.7% | 5.9% |
| LSOA | | | 1.9% | 1.7% | 0.5% | 0.5% |
| Family | 59.8% | | 40.4% | | 42.0% | |
| Pupil | 40.2% | 86.1% | 37.7% | 80.8% | 40.1% | 84.2% |

Research questions

1. How much of the shared environmental variation is due to family, school and area?
2. How much of the 'pupil' level variation in school effectiveness studies is really family level?

What happens when we try to explain some of the variation using pupil, family and LSOA level covariates?

Results

| | Model A | | Model B | | Model C | | Model D | |
|------------------|---------|---------|---------|---------|---------|---------|---------|---------|
| cons | -0.003 | (0.001) | -0.003 | (0.001) | 0.001 | (0.008) | -0.039 | (0.007) |
| twin | 0.177 | (0.008) | 0.179 | (0.007) | 0.162 | (0.007) | 0.154 | (0.007) |
| pretest | 0.730 | (0.001) | 0.729 | (0.001) | 0.701 | (0.001) | 0.641 | (0.001) |
| pretest.twin | -0.040 | (0.007) | 0.000 | (0.007) | -0.027 | (0.006) | -0.020 | (0.006) |
| female | | | | | | | 0.184 | (0.002) |
| Asian | | | | | | | 0.429 | (0.005) |
| Black | | | | | | | 0.225 | (0.006) |
| Chinese | | | | | | | 0.556 | (0.015) |
| Mixed | | | | | | | 0.045 | (0.005) |
| Other | | | | | | | 0.403 | (0.010) |
| FSM | | | | | | | -0.248 | (0.003) |
| age | | | | | | | -0.012 | (0.000) |
| SEN | | | | | | | -0.231 | (0.003) |
| IDACI | | | | | | | -0.103 | (0.001) |
| LEA | | | | | 0.005 | (0.001) | 0.005 | (0.001) |
| Secondary | | | 0.065 | (0.002) | 0.043 | (0.001) | 0.035 | (0.001) |
| Primary | | | | | 0.035 | (0.001) | 0.025 | (0.000) |
| LSOA | | | | | 0.008 | (0.000) | 0.002 | (0.000) |
| Family (twin) | 0.238 | (0.007) | | | 0.168 | (0.005) | 0.157 | (0.005) |
| Pupil (twin) | 0.160 | (0.003) | | | 0.157 | (0.003) | 0.150 | (0.003) |
| Pupil (non-twin) | 0.468 | (0.001) | 0.402 | (0.002) | 0.383 | (0.001) | 0.357 | (0.001) |

Using MCMC; 450,500 iterations and a burn-in of 50,000

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels

Interpretation

Summary

- ▣ Around a third of the family level variation in Model A is really school or area level (mostly school)
- ▣ Around half the pupil level variation in Model B is really family level
- ▣ The covariates explain some variation at most levels
- ▣ Family and pupil still make up the largest, roughly equal proportions of variation

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Caveats

- Our family effects are purely derived from twin pairs

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Caveats

- Our family effects are purely derived from twin pairs
- The twins are a mix of MZ and DZ so we are not estimating $\sigma_u^2 + \sigma_g^2$

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Caveats

- Our family effects are purely derived from twin pairs
- The twins are a mix of MZ and DZ so we are not estimating $\sigma_u^2 + \sigma_g^2$
- Twins may be different to full sibling pairs

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Caveats

- Our family effects are purely derived from twin pairs
- The twins are a mix of MZ and DZ so we are not estimating $\sigma_u^2 + \sigma_g^2$
- Twins may be different to full sibling pairs
 - shared environment in the womb

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Caveats

- Our family effects are purely derived from twin pairs
- The twins are a mix of MZ and DZ so we are not estimating $\sigma_u^2 + \sigma_g^2$
- Twins may be different to full sibling pairs
 - shared environment in the womb
 - they may elicit more similar environments

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Caveats

- Our family effects are purely derived from twin pairs
- The twins are a mix of MZ and DZ so we are not estimating $\sigma_u^2 + \sigma_g^2$
- Twins may be different to full sibling pairs
 - shared environment in the womb
 - they may elicit more similar environments
 - have same age sibling

Interpretation

Summary

- Around a third of the family level variation in Model A is really school or area level (mostly school)
- Around half the pupil level variation in Model B is really family level
- The covariates explain some variation at most levels
- Family and pupil still make up the largest, roughly equal proportions of variation
- Both school levels also remain important

Caveats

- Our family effects are purely derived from twin pairs
- The twins are a mix of MZ and DZ so we are not estimating $\sigma_u^2 + \sigma_g^2$
- Twins may be different to full sibling pairs
 - shared environment in the womb
 - they may elicit more similar environments
 - have same age sibling
- To what extent can we generalise to other family types?
 - e.g. single child families

2. What happens under stress?

Variance functions for stress

Data

- Data is from previous cohort, who took GCSEs in 2006

Model

Variance functions for stress

Data

- Data is from previous cohort, who took GCSEs in 2006
- Postcodes with more than 2 students excluded

Model

Variance functions for stress

Data

- ▣ Data is from previous cohort, who took GCSEs in 2006
- ▣ Postcodes with more than 2 students excluded
- ▣ Continuous variables not standardized

Model

Variance functions for stress

Data

- Data is from previous cohort, who took GCSEs in 2006
- Postcodes with more than 2 students excluded
- Continuous variables not standardized

Stressors

- Our main stressor was IDACI, an LSOA level variable

Model

Variance functions for stress

Data

- Data is from previous cohort, who took GCSEs in 2006
- Postcodes with more than 2 students excluded
- Continuous variables not standardized

Stressors

- Our main stressor was IDACI, an LSOA level variable
- It aims to measure income deprivation affecting children

Model

Variance functions for stress

Data

- Data is from previous cohort, who took GCSEs in 2006
- Postcodes with more than 2 students excluded
- Continuous variables not standardized

Stressors

- Our main stressor was IDACI, an LSOA level variable
- It aims to measure income deprivation affecting children
- Other stressors included:
 - FSM eligibility
 - House moves

Model

Variance functions for stress

Data

- Data is from previous cohort, who took GCSEs in 2006
- Postcodes with more than 2 students excluded
- Continuous variables not standardized

Stressors

- Our main stressor was IDACI, an LSOA level variable
- It aims to measure income deprivation affecting children
- Other stressors included:
 - FSM eligibility
 - House moves

Model

$$\begin{aligned} \text{GCSE}_{ijk} = & \alpha + \beta_1 \text{pretest}_{ijk} + \beta_2 \text{twin}_{jk} + \beta_5 \text{stressor}_{jk} \\ & + v_{0k} + u_{2jk} \text{twin}_{jk} + e_{2ijk} \text{twin}_{jk} + e_{3ijk} \text{nontwin}_{jk} \\ & + u_{4jk} \text{twin} \cdot \text{stressor}_{jk} + e_{4ijk} \text{twin} \cdot \text{stressor}_{jk} \\ & + e_{6ijk} \text{nontwin} \cdot \text{stressor}_{jk} \end{aligned}$$

Variance functions for stress

Covariance structure

$$\begin{aligned} [v_{0k}] &\sim N(0, [\sigma_{v0}^2]) \\ \begin{bmatrix} u_{2jk} \\ u_{4jk} \end{bmatrix} &\sim N\left(0, \begin{bmatrix} \sigma_{u2}^2 & \\ \sigma_{u24} & \sigma_{u4}^2 \end{bmatrix}\right) \\ \begin{bmatrix} e_{2ijk} \\ e_{3ijk} \\ e_{4ijk} \\ e_{6ijk} \end{bmatrix} &\sim N\left(0, \begin{bmatrix} \sigma_{e2}^2 & & & \\ 0 & \sigma_{e3}^2 & & \\ \sigma_{e24} & 0 & \sigma_{e4}^2 & \\ 0 & \sigma_{e36} & 0 & \sigma_{e6}^2 \end{bmatrix}\right) \end{aligned}$$

Model

$$\begin{aligned} \text{GCSE}_{ijk} &= \alpha + \beta_1 \text{pretest}_{ijk} + \beta_2 \text{twin}_{jk} + \beta_5 \text{stressor}_{jk} \\ &+ v_{0k} + u_{2jk} \text{twin}_{jk} + e_{2ijk} \text{twin}_{jk} + e_{3ijk} \text{nontwin}_{jk} \\ &+ u_{4jk} \text{twin} \cdot \text{stressor}_{jk} + e_{4ijk} \text{twin} \cdot \text{stressor}_{jk} \\ &+ e_{6ijk} \text{nontwin} \cdot \text{stressor}_{jk} \end{aligned}$$

Variance functions for stress

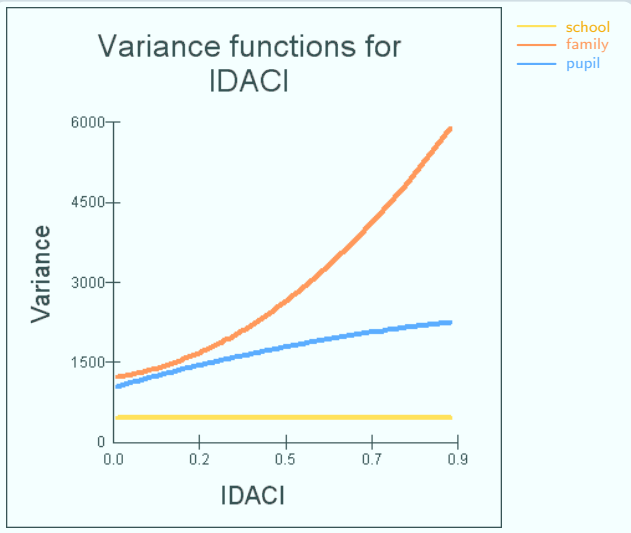
Covariance structure

$$\begin{aligned} [v_{0k}] &\sim N(0, [\sigma_{v0}^2]) \\ \begin{bmatrix} u_{2jk} \\ u_{4jk} \end{bmatrix} &\sim N\left(0, \begin{bmatrix} \sigma_{u2}^2 & \\ \sigma_{u24} & \sigma_{u4}^2 \end{bmatrix}\right) \\ \begin{bmatrix} e_{2ijk} \\ e_{3ijk} \\ e_{4ijk} \\ e_{6ijk} \end{bmatrix} &\sim N\left(0, \begin{bmatrix} \sigma_{e2}^2 & & & \\ 0 & \sigma_{e3}^2 & & \\ \sigma_{e24} & 0 & \sigma_{e4}^2 & \\ 0 & \sigma_{e36} & 0 & \sigma_{e6}^2 \end{bmatrix}\right) \end{aligned}$$

Model

$$\begin{aligned} \text{GCSE}_{ijk} = & \alpha + \beta_1 \text{pretest}_{ijk} + \beta_2 \text{twin}_{jk} + \beta_5 \text{IDACI}_{jk} \\ & + v_{0k} + u_{2jk} \text{twin}_{jk} + e_{2ijk} \text{twin}_{jk} + e_{3ijk} \text{nontwin}_{jk} \\ & + u_{4jk} \text{twin} \cdot \text{IDACI}_{jk} + e_{4ijk} \text{twin} \cdot \text{IDACI}_{jk} \\ & + e_{6ijk} \text{nontwin} \cdot \text{IDACI}_{jk} \end{aligned}$$

Results



Interpreting the results

As IDACI increases,

We have this situation:



Interpreting the results

As IDACI increases,

- The mean progress decreases

- $\beta_5 = -68.1$

We have this situation:



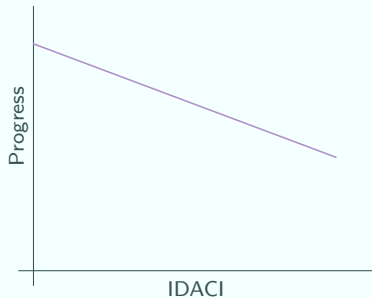
Interpreting the results

As IDACI increases,

- The mean progress decreases

- $\beta_5 = -68.1$

We have this situation:



Interpreting the results

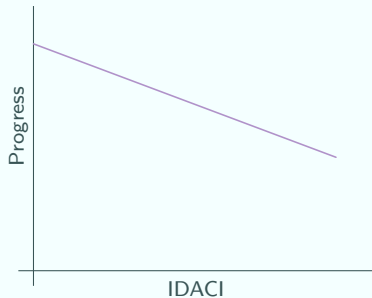
As IDACI increases,

- Between family variation increases

- The mean progress decreases

- $\beta_5 = -68.1$

We have this situation:



Interpreting the results

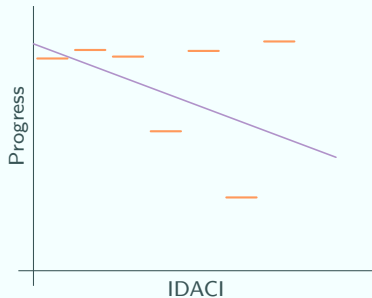
As IDACI increases,

- Between family variation increases

- The mean progress decreases

- $\beta_5 = -68.1$

We have this situation:

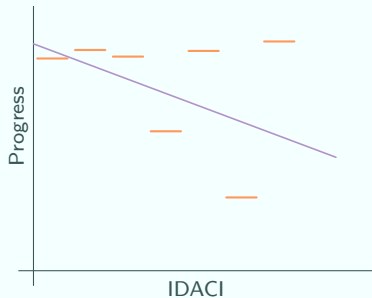


Interpreting the results

As IDACI increases,

- **Between family** variation increases
- **Within family** variation increases
- The **mean** progress decreases
 - $\beta_5 = -68.1$

We have this situation:

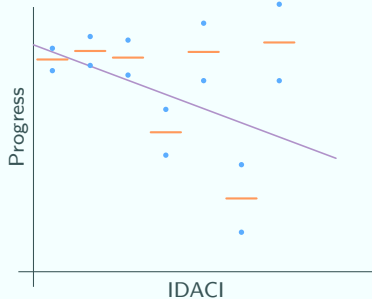


Interpreting the results

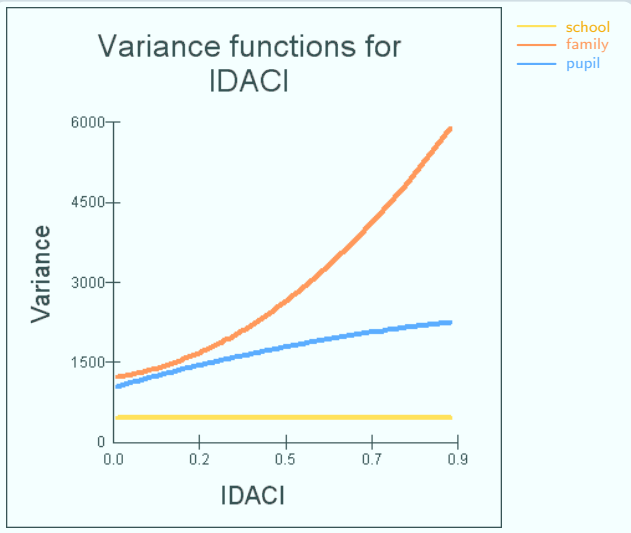
As IDACI increases,

- **Between family** variation increases
- **Within family** variation increases
- The **mean** progress decreases
 - $\beta_5 = -68.1$

We have this situation:



Results

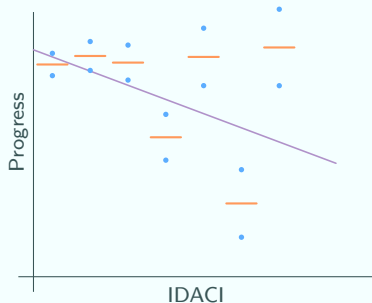


Interpreting the results

As IDACI increases,

- **Between family** variation increases
- **Within family** variation increases
- The **mean** progress decreases
 - $\beta_5 = -68.1$

We have this situation:



- Between family variation increases more dramatically than within family variation
- So at greater levels of deprivation, family becomes relatively more important in determining progress

Other stressors

- We fitted the same model with different stressors:

Other stressors

- We fitted the same model with different stressors:
 - IMD

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house
 - Number of house moves

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house
 - Number of house moves
 - Time since house move

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house
 - Number of house moves
 - Time since house move
- In almost all cases we see the same pattern

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house
 - Number of house moves
 - Time since house move
- In almost all cases we see the same pattern
- We also fitted models with more than one stressor

Other stressors

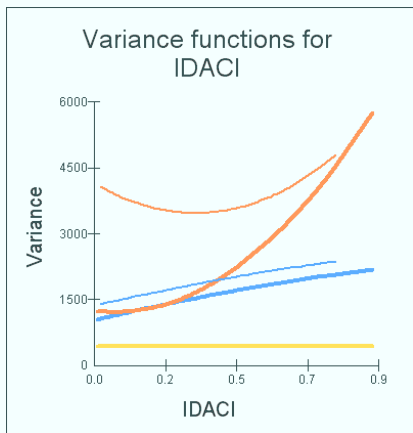
- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house
 - Number of house moves
 - Time since house move
- In almost all cases we see the same pattern
- We also fitted models with more than one stressor
 - e.g. IDACI and FSM eligibility

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house
 - Number of house moves
 - Time since house move
- In almost all cases we see the same pattern
- We also fitted models with more than one stressor
 - e.g. IDACI and FSM eligibility
- In these models, both stressors show the same pattern

Other stressors

- We fitted the same model with different stressors:
 - IMD
 - FSM eligibility
 - Ever moved house
 - Number of house moves
 - Time since house move
- In almost all cases we see the same pattern
- We also fitted models with more than one stressor
 - e.g. IDACI and FSM eligibility
- In these models, both stressors show the same pattern



— school
— family
— pupil
— nonFSM
— FSM

What's going on? Possible explanations

Genetic explanation

- **Some families** have genes which help to maintain progress in the presence of stressors, while others do not

Environmental explanation

What's going on? Possible explanations

Genetic explanation

- **Some families** have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability

Environmental explanation

What's going on? Possible explanations

Genetic explanation

- **Some families** have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some **families** have the gene and some don't

Environmental explanation

What's going on? Possible explanations

Genetic explanation

- Within families, some children have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some children have the gene and some don't

Environmental explanation

What's going on? Possible explanations

Genetic explanation

- Within families, some children have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some children have the gene and some don't

Environmental explanation

- Some families, across all levels of the stressors, have factors that make it harder to be good parents
 - alcoholism of parent
 - violent spouse

What's going on? Possible explanations

Genetic explanation

- Within families, some children have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some children have the gene and some don't

Environmental explanation

- Some families, across all levels of the stressors, have factors that make it harder to be good parents
 - alcoholism of parent
 - violent spouse
- In the absence of stressors, even families with these factors can provide a good environment for progress

What's going on? Possible explanations

Genetic explanation

- Within families, some children have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some children have the gene and some don't

Environmental explanation

- Some families, across all levels of the stressors, have factors that make it harder to be good parents
 - alcoholism of parent
 - violent spouse
- In the absence of stressors, even families with these factors can provide a good environment for progress
- In the presence of stressors, families with these factors cannot do so → variability since some families have these factors and some don't

What's going on? Possible explanations

Genetic explanation

- Within families, some children have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some children have the gene and some don't

Environmental explanation

- Children in families compete for resources

What's going on? Possible explanations

Genetic explanation

- Within families, some children have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some children have the gene and some don't

Environmental explanation

- Children in families compete for resources
- In the absence of stressors, there are enough resources for the needs of all children

What's going on? Possible explanations

Genetic explanation

- Within families, some children have genes which help to maintain progress in the presence of stressors, while others do not
- In the absence of a stressor, the genes make little difference so there is not much variability
- In the presence of a stressor, the genes make a big difference so there is variability arising from the fact that some children have the gene and some don't

Environmental explanation

- Children in families compete for resources
- In the absence of stressors, there are enough resources for the needs of all children
- In the presence of stressors, there are fewer resources and some children will have their needs met while others will not → variability since those getting more resources can make more progress

References

References

- Brooks, A., Fulker, D. W. and DeFries, J. C. (1990) Reading performance and general cognitive ability: A multivariate analysis of twin data. *Personality and Individual Differences*, **11**:2, 141–146
- Cardon, L. R., Fisher DiLalla, L., Plomin, R., DeFries, J. C. and Fulker, D. W. (1990) Genetic correlations between reading performance and IQ in the Colorado Adoption Project. *Intelligence* **14**, 245–257
- Cleveland, H. H., Jacobson, K. C., Lipinski, J. J. and Rowe, D. C. (2000) Genetic and shared environmental contributions to the relationship between the home environment and child and adolescent achievement. *Intelligence* **28**:1 69–86
- Duncan, G. J., Boisjoly, J. and Mullan Harris, K. (2001) Sibling, peer, neighbourhood and schoolmate correlations as indicators of the importance of context for adolescent development. *Demography* **38**(3): 437–447
- Fielding, A., Thomas, H., Steele, F., Browne, W., Leyland, A., Spencer, N. and Davison, I. (2006) Using Cross-Classified Multilevel Models to Improve Estimates of the Determination of Pupil Attainment: A Scoping Study. Research Report for Department for Education and Skills. School of Education, University of Birmingham, ISBN: 9780704426016 (International) 0704426013 (UK)
- Friend, A., DeFries, J. C., Wadsworth, S. J. and Olson, R. K. (2007) Genetic and environmental influences on word recognition and spelling deficits as a function of age. *Behavior Genetics* **37**, 477–486
- Garner, C. and Raudenbush, S. W. (1991) Neighbourhood effects on educational attainment. *Sociology of Education*, **64**, 251–262
- Goldstein, H., Burgess, S. and McConnell, B. (2007) Modelling the effect of pupil mobility on school differences in educational achievement. *J. R. Statist. Soc. A*, **170**, 941–954
- Haworth, C. M. A., Kovas, Y., Petrill, S. A. and Plomin, R. (2007) Developmental origins of low mathematics performance and normal variation in twins from 7 to 9 years. *Twin Research and Human Genetics* **10**:1, 106–117
- Haworth, C. M. A., Kovas, Y., Dale, P. S. and Plomin, R. (2008) Science in elementary school: Generalist genes and school environments. *Intelligence* **36**, 694–701
- Leckie, G. (2009) The complexity of school and neighbourhood effects and movements of pupils on school differences in models of educational achievement. *J. R. Statist. Soc A* (forthcoming)

References

- Petrill, S. A. and Thompson, L. A. (1993) The phenotypic and genetic relationships among measures of cognitive ability, temperament, and scholastic achievement. *Behavior Genetics* **23**:6, 511–518
- Petrill, S. A. and Thompson, L. A. (1994) The effect of gender upon heritability and common environmental estimates in measures of scholastic achievement. *Personality and Individual Differences* **16**:4 631–640
- Raudenbush, S. W. (1993) A crossed random effects model for unbalanced data with applications in cross-sectional and longitudinal research. *J. Educ. Statist.*, **18**, 321–349
- Thompson, L. A., Detterman, D. K. and Plomin, R. (1991) Associations between cognitive abilities and scholastic achievement: Genetic overlap but environmental differences. *Psychological Science* **2**:3, 158–165
- Thompson, L. A., Detterman, D. K. and Plomin, R. (1993) Differences in heritability across groups differing in ability, revisited. *Behavior Genetics* **23**:4, 331–336
- Van den Oord, E. J. C. G. and Rowe, D. C. (1997) An examination of genotype-environment interactions for academic achievement in an U.S. national longitudinal survey. *Intelligence* **25**:3 205–228
- Wainwright, M. A., Wright, M. J., Geffen, G. M., Luciano, M. and Martin, N. G. (2005) The genetic basis of academic achievement on the Queensland Core Skills Test and its shared genetic variance with IQ. *Behavior Genetics* **35**:2 133–145
- Yang, M. and Woodhouse, G. (2001) Progress from GCSE to A and AS level: institutional and gender differences, and trends over time. *British Educational Research Journal*, **27**, 245–267